## Glycemic Variability Measures Evan Olawsky

11/15/2019

This document details the calculations made in the R script GV measures.R. That script is based upon the Easy GV spreadsheet constructed by Dr. Nathan R. Hill of Oxford University. In many cases, Easy GV does not give results consistent with the formulas presented in the original manuscripts. In these cases, GV measures.R gives an option to calculate either the Easy GV version or the original manuscript option.

Throughout this document, let  $X_t$  be a glucose reading at time t. Let n be the total number of glucose readings. Time is assumed to be measured in minutes since the first recording in the data set. Glucose readings can be measured in either mg/dL or mmol/L. Note that 1 mmol of glucose is equal to 18 mg of glucose.

All functions require a vector **x** of glucose readings. This vector should be numeric and should not include any blank entries. Some functions additionally require a vector **times** of times. This vector should also be numeric and should not include any blank entries. Currently, the function **read**.CGM can take a Dexcom output file as input and return a data.frame which includes properly formatted **x** and **times** vectors.

The wrapper function GV returns all of the following metrics simultaneously.

# Continuous overall net glycemic action (CONGA) (McDonell et al. 2005)

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- n, the number of hours between "partner" observations. Null value is 1.
- s, the number of minutes of slack used when searching for partners. Null value is 1.
- method, either "manuscript" or "easy". Null value is "manuscript".

For a glucose measurement  $X_t$  at time t, let  $D_t$  be the difference between  $X_t$  and the mean of all glucose measurements made n hours prior to  $X_t$ , plus or minus s minutes. Let T be the set of times with a  $D_t$  value and let k be the number of such observations. Finally, let  $\overline{D} = \sum D_t/k$ . Then, the original manuscript version is

$$CONGA_M(n) = \sqrt{\frac{\sum_T (D_t - \bar{D})^2}{k - 1}}$$

Furthermore, let  $\overline{D}^* = \sum |D_t|/k$ . Then the Easy GV version is

$$CONGA_{GV}(n) = \sqrt{\frac{\sum_{T} (X_t - \bar{D}^*)^2}{k - 1}}$$

### Lability Index (LI) (Ryan et al. 2004)

- x, a vector of glucose readings
- times, a vector of corresponding times
- k, length of time (in minutes) used to find partners. Null value is 60.
- s, the number of minutes of slack used when searching for partners. Null value is 1.

For a glucose measurement  $X_t$  at time t, let  $D_t$  be the difference between  $X_t$  and the mean of all glucose measurements made k minutes prior to  $X_t$ , plus or minus s minutes. Let T be the set of times with a  $D_t$  value and let k be the number of such observations. Then

$$LI = \frac{1}{k} \sum_{t \in T} (D_t)^2$$

### J-index (Wojcicki 1995)

Parameters include

- x, a vector of glucose readings
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".

Let X be the mean of all glucose values, and let SD(X) be the standard deviation of all glucose values. If the units are mg/dL,

$$J = \frac{1}{1000} (\bar{X} + SD(X))^2$$

and if the units are mmol/L,

$$J = \frac{18^2}{1000} (\bar{X} + SD(X))^2$$

# Low / High Blood Glucose Index (LBGI, HBGI) (Kovatchev et al. 2003) and (Gaynanova, Urbanek, and Punjabi 2018)

Parameters include

- x, a vector of glucose readings
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".
- method, one of "manuscript", "easy", or "corrected". Null value is "manuscript". "Corrected" refers to the Gaynanova paper's recommendation.

If the units are mg/dL, let  $f(x) = 1.509(\ln(x)^{1.084} - 5.381)$ . If the units are mmol/L, let  $f(x) = 1.509(\ln(18x)^{1.084} - 5.381)$ . Let  $rl(x) = cf(x)^2$  when f(x) < 0 and rl(x) = 0 otherwise. Let  $rh(x) = cf(x)^2$  when f(x) > 0 and rh(x) = 0 otherwise. In the original manuscript, Kovatchev et al use c = 10. Gaynanova et al recommend c = 22.77. Both measures can be obtained from this code, by setting method to corrected or manuscript, respectively. Then, the original manuscript version is

$$LBGI_M = \frac{\sum rl(x_t)}{n}$$
$$HBGI_M = \frac{\sum rh(x_t)}{n}$$

where n is the total number of glucose readings.

The Easy GV version is

$$LBGI_{GV} = \frac{\sum rl(x_t)}{\sum I(rl(x_t) > 0)}$$
$$HBGI_{GV} = \frac{\sum rh(x_t)}{\sum I(rh(x_t) > 0)}$$

# Glycemic Risk Assessment Diabetes Equation (GRADE) (Hill et al. 2007)

Parameters include

- x, a vector of glucose readings
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".
- method, either "manuscript" or "easy". Null value is "manuscript".
- c1, the glucose value below which readings are considered hypoglycemic
- c2, the glucose value above which readings are considered hyperglycemic

If the units are mg/dL, let

$$g(x) = \min(425[\log(\log(x/18)) + C]^2, 50)$$

If the units are mmol/L, let

$$g(x) = \min(425[\log(\log(x)) + C]^2, 50)$$

Where the logarithm is base ten in both cases. Let C = 1.6 for the manuscript calculation and let C = 1.5554147 for the Easy GV calculation.

For the manuscript calculation,  $GRADE_M$  is the mean of the  $g(x_t)$ . For the Easy GV calculation,  $GRADE_{GV}$  is the median of the  $g(x_t)$ .

We also calculate the contributions of hypoglycemia, euglycemia, and hyperglycemia to the GRADE score.

Hypo percentage 
$$= \frac{\sum\limits_{x_t < C_1} g(x_t)}{\sum\limits_{\text{all } x_t} g(x_t)}$$
Eu percentage 
$$= \frac{\sum\limits_{x_t < C_2} g(x_t)}{\sum\limits_{\text{all } x_t} g(x_t)}$$
Hyper percentage 
$$= \frac{\sum\limits_{x_t > C_2} g(x_t)}{\sum\limits_{\text{all } x_t} g(x_t)}$$

If the units are mg/dL, the default values for  $C_1$  and  $C_2$  are 70.2 and 140.4\$ If the units are mmol/L, the defaults are 3.9 and 7.8.

#### Mean of Daily Differences (MODD) (Molnar, Taylor, and Ho 1972)

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- s, the number of minutes of slack used when searching for partners. Null value is 1.
- method, either "manuscript" or "easy". Null value is "manuscript".

For a glucose measurement  $X_t$  at time t, let  $D_t$  be the difference between  $X_t$  and the mean of all glucose measurements made 24 hours prior to  $X_t$ , plus or minus s minutes. Let T be the set of times with a  $D_t$  value and let k be the number of such observations.

Then, the original manuscript version is

$$MODD_M = \frac{1}{k} \sum_T |D_t|$$

Let  $T^- = T \setminus max(t \in T)$ . Then, the Easy GV version is

$$MODD_{GV} = \frac{1}{K-1} \sum_{T^-} |D_t|$$

# Mean Amplitude of Glycemic Excursions (MAGE) (Service et al. 1970)

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times

Note that the original manuscript for MAGE is not very precise and does not lead to an obvious calculation of MAGE. While Easy GV does not appear to calculate MAGE in the same way as the original manuscript, the Easy GV version of MAGE is the only one we present here.

Let  $D_t = X_t - X_{t-1}$ . Then let E be the set of all  $D_t$  whose absolute value exceeds the standard deviation of all glucose readings from the day that  $D_t$  occurred. Then let  $E^+$  be the set that contains the positive  $D_t$  values in E, with size  $\#E^+$ . Let  $E^-$  be the set that contains the negative  $D_t$  values in E, with size  $\#E^+$ . We then report separate positive and negative MAGE values:

$$MAGE_{+} = \frac{1}{\#E^{+}} \sum_{E^{+}} D_{t}$$
$$MAGE_{-} = \frac{1}{\#E^{-}} \sum_{E^{-}} D_{t}$$

#### Average Daily Risk Range (ADRR) (Kovatchev et al. 2006)

- x, a vector of glucose readings
- times, a vector of corresponding times

- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".
- method, either "manuscript" or "easy". Null value is "manuscript".

If the units are mg/dL, let

$$f(x) = [1.509(\ln(x)^{1.084} - 5.381)]$$

If the units are mmol/L, let

$$f(x) = [1.509(\ln(18x)^{1.084} - 5.381)]$$

Let  $rl(x) = 10f(x)^2$  when f(x) < 0 and rl(x) = 0 otherwise. Let  $rh(x) = 10f(x)^2$  when f(x) > 0 and rh(x) = 0 otherwise. Denote  $(x_1^d, \ldots, x_{n_d}^d)$  as the  $n_d$  glucose values on day d. Then let

$$LR^d = \max(rl(x_1^d), \dots, rl(x_{n_d}^d))$$

and

$$HR^{d} = max(rh(x_{1}^{d}), \dots, rh(x_{n_{d}}^{d}))$$

for day d. Let D be the total number of days where glucose levels were measured. Then, the original manuscript version is

$$ADRR_M = \frac{1}{D} \sum_{d=1}^{D} (LR^d + HR^d)$$

The Easy GV version gives high and low measures separately.

$$ADRR_{L} = \frac{1}{D} \sum_{d=1}^{D} (LR^{d})$$
$$ADRR_{H} = \frac{1}{D} \sum_{d=1}^{D} (HR^{d})$$

#### M-value (Schlichtkrull, Munck, and Jersild 1965)

Parameters include

- x, a vector of glucose readings
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".
- index, a value to be considered a 'standard' blood glucose value, in mg/dL. Null value is 120.
- method, either "manuscript" or "easy". Null value is "manuscript".

After conversion of all glucose values to mg/dL, let  $M^* = (10\log \frac{x}{\text{index}})^3$  and let  $W = (max(x_i) - min(x_i))/20$ . The log used in that equation is base 10.

Then, the original manuscript version is

$$M_M = \frac{1}{N} \sum_{i=1}^{N} |M^*| + W$$

The Easy GV version is

$$M_{GV} = \frac{1}{N} \sum_{i=1}^{N} |M^*|$$

### Mean Absolute Glucose (MAG) (Hermanides et al. 2010)

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times

$$MAG = \frac{\sum_{i=1}^{N-1} |x_{i+1} - x_i|}{(\max(t) - \min(t))/60}$$

where N is the total number of glucose values.

### Coefficient of variation (CV)

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- overall, a logical, equal to TRUE you want the CV for the entire dataset, or equal to FALSE if you would prefer many CV values over a moving window
- interval, size (in hours) of the moving window to be used if overall is false. Null value is 1.

$$CV = SD(X)/\bar{X},$$

where X is a vector of glucose readings, potentially restricted to a particular time window.

### Standard deviation (SD)

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- overall, a logical, equal to TRUE you want the SD for the entire dataset, or equal to FALSE if you would prefer many SD values over a moving window
- interval, size (in hours) of the moving window to be used if overall is false. Null value is 1.

$$SD = \sqrt{\frac{1}{N-1} \sum_{t \in T} (x_t - \bar{x})^2},$$

where T is a set of times (potentially restricted to a particular window) and N is the size of T.

### Area Under the Curve (AUC)

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- thresh, a threshold above (or below) which you wish to calculate the AUC. Default is 100.
- above, a logical indicating whether you wish to calculate area above the threshold value (TRUE) or below it (FALSE). Default is TRUE.

If above == T,

If above == F,

$$AUC_{-} = -\sum_{i=1}^{N-1} I(x_i \le \nu) I(x_{i+1} \le \nu) \Big( \min(x_i - \nu, x_{i+1} - \nu)(t_{i+1} - t_i) + |x_{i+1} - x_i|(t_{i+1} - t_i)/2 \Big) \Big)$$

where  $\nu$  is the threshold value and N is the length of the glucose vector.

For each excursion beyond this threshold value, this calculation does not include the triangular area from the threshold to the first glucose value beyond the threshold, nor from the last glucose beyond the threshold back to the threshold. Hence a single glucose value beyond the threshold is not captured by the calculation.

### Time spent in range (TIR) (Battelino and others 2019)

Parameters include

- x, a vector of glucose readings
- low, the lower bound of the range
- high, the upper bound of the range

This function gives the percentage of glucose readings that fall in a given range (l, u).

$$TIR = \sum_{i=1}^{N} I(l \le x_i \le u)/N$$

Battelino et al suggest five ranges: below 54 mg/dL, 55-70, 71-180, 181-250, above 250.

# Glucose Management Indicator (GMI) (Bergenstal and others 2018)

- x, a vector of glucose readings
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".

Let  $\bar{x}$  be the mean of all glucose readings taken. If the units are mg/dL, then

 $GMI = 3.31 + 0.02392\bar{x}$ 

If the units are mmol/L,

$$12.71 + 4.70587\bar{x}$$

#### Number of episodes per day

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- thresh, a threshold, where glucoses below the threshold are considered as part of an episode
- len, the minimum length of an episode
- gap, the typical gap between CGM measurements, in minutes

This function counts the number of "episodes" where glucose values remain below a certain threshold thresh for a period of at least len minutes. Then the number of episodes is divided by the amount of days that the sensor was active. This amount is calculated by taking the total time (the time between the first and last measurements), subtracting any gaps in time that are longer than gap+2 minutes and then adding back gap minutes for each of the gaps subtracted away.

#### Other functions

#### read.CGM

- file, the name of the file (in CSV format) to be read-in
- timezero, set to "first" if the first glucose reading should be considered time zero and set to "midnight" if midnight of the day of the first reading should be considered time zero. Default is "first".
- na.rm, a logical that is TRUE if you wish to exclude all readings that are missing glucose values or time stamps and FALSE if not. Default is TRUE.
- skip, the number of lines in the data file to skip before beginning to read in data
- calib.col, the number or name of the column containing information regarding calibration status of each glucose entry
- calib.tag, the character value used to denote calibration rows in calib.col
- mult.sensors, a logical that is TRUE if you wish to split the data set into parts corresponding to different CGM sensors and FALSE if not. Default is FALSE.
- sensor.times, a vector of times (in the same format as the time data) that correspond to the beginning of a new CGM sensor. These times are used to split the data between multiple sensors if mult.sensors is TRUE. If sensor.times is NA, the data is split automatically at every gap of sensor.gap or more minutes.
- sensor.gaps, a number specifying the minimum gap (in minutes) for which we should split the data into two pieces. Default is 120.
- time.col, the number or name of the column containing time data
- gluc.col, the number or name of the column containing glucose data
- time.sep, character that separates date from time in your time data

- time.format, specify date and time formats according to the specification used in the chron package. Default is c(dates = "m/d/y", times = "h:m:s").
- high.ind, character value that identifies high glucose values in the data. Default is "High".
- high.value, numeric value by which to replace glucose values equal to high.ind. Default is 400.
- low.ind, character value that identifies low glucose values in the data. Default is "Low".
- low.value, numeric value by which to replace glucose values equal to low.ind. Default is 40.

This function takes in data from a CGM and converts it into a data frame with one column of glucose readings and one column of times (in minutes). These two columns can then be used with any of the glucose variability functions.

#### plot.CGM

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".

This function returns a plot of blood glucose over time.

#### plot.diff

Parameters include

- x, a vector of glucose readings
- times, a vector of corresponding times
- n, the number of hours between "partner" observations. Null value is 1.
- s, the number of minutes of slack used when searching for partners. Null value is 1.
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".

This function returns a plot of the n-hour changes in glucose values over time.

#### plot.symm

Parameters include

- $\boldsymbol{x},$  a vector of glucose readings
- times, a vector of corresponding times
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".

This function returns a plot of the "symmetrized" glucose values used in calculating BGI and ADRR.

#### $\mathbf{GV}$

- x, a vector of glucose readings
- times, a vector of corresponding times
- unit, either "mg" if the units are mg/dL or "mmol" if the units are mmol/L. Null value is "mg".
- m.index, a value to be considered a 'standard' blood glucose value, in mg/dL. Null value is 120.
- k, length of time (in minutes) used to find partners. Null value is 60.
- s, the number of minutes of slack used when searching for partners. Null value is 1.
- conga.n, the number of hours between "partner" observations. Null value is 1.

- interval, size (in hours) of the moving window to be used if overall is false. Null value is 1.
- thresh, a threshold above (or below) which you wish to calculate percentages. Default is 100

This is a wrapper function that outputs a table with all 14 metrics, calculated for both manuscript and Easy GV methods, if applicable.

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